## Probability and Random Processes ECS 315

## Asst. Prof. Dr. Prapun Suksompong

prapun@siit.tu.ac.th<br>6.1 Conditional Probability



## Office Hours:

BKD, 6th floor of Sirindhralai building
Wednesday 14:00-15:30
Friday 14:00-15:30

Suppose we have a diagnostic test for a particular disease which is $99 \%$ accurate. The test gives a positive result.


What is the probability that the person actually has the disease?

## News: September 2015



## Disease Testing

- Suppose we have a diagnostic test for a particular disease which is $99 \%$ accurate.
- A person is picked at random and tested for the disease.
- The test gives a positive result.
- Q1: What is the probability that the person actually has the disease?
- Natural answer: $99 \%$ because the test gets it right $99 \%$ of the times.



## 99\% accurate test?

- Two kinds of error
- If you use this test on many persons with the disease, the test will indicate correctly that those persons have disease $99 \%$ of the time.
- False negative rate $=1 \%=0.01$

$$
1 \rightarrow 0
$$

- If you use this test on many persons without the disease, the test will indicate correctly that those persons do not have disease $99 \%$ of the time.
- False positive rate $=1 \%=0.01$

$$
0 \rightarrow 1
$$

## False positive and false negative

Type I error
(false positive)


Type II error
(false negative)


## Disease Testing: The Question

- Suppose we have a diagnostic test for a particular disease which is $99 \%$ accurate.
- A person is picked at random and tested for the disease.
- The test gives a positive result.
- Q1: What is the probability that the person actually has the disease?
- Natural answer: $99 \%$ because the test gets it right $99 \%$ of the times.
- Q2: Can the answer be $1 \%$ or $2 \%$ ?
- Q3: Can the answer be $50 \%$ ?


## Disease Testing: The Answer

Q1: What is the probability that the person actually has the disease?

A1: The answer actually depends on how common or how rare the disease is!


## Why?

- Let's assume rare disease.
- The disease affects about 1 person in 10,000.
- Try an experiment with $10^{6}$ people.
- Approximately $\mathbf{1 0 0}$ people will have the disease.
- What would the ( $99 \%$-accurate) test say?



## Results of the test



## Results of the test



99 of them will test positive 1 of them will test negative

100 people w/ disease
Of those who test positive, only $\frac{99}{99+9,999} \approx 1 \%$ actually have the disease!


989,901 of them will test negative
9,999 of them will test positive

